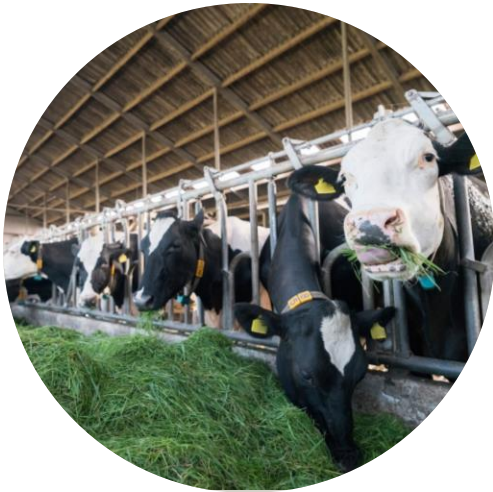


# Cross-Validation Assessment of Random Regression Models for Dry Matter Intake

Interbull Annual Meeting  
Bled, 2024

Matias F. Schrauf, Birgit Gredler-Grandl, Renzo Bonifazi, Jeremie Vandenplas, Jan ten Napel,  
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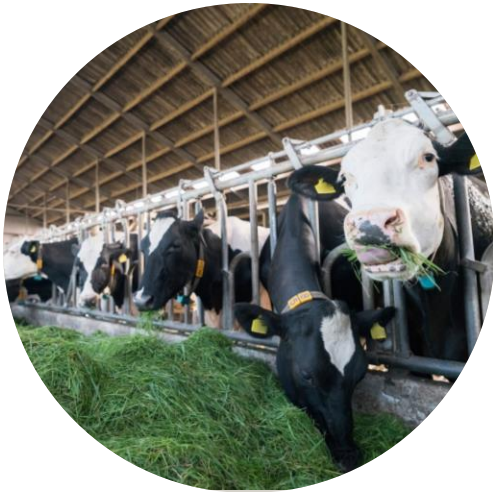
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# Dry Matter Intake

# Genetic Evaluation for Dry Matter Intake (DMI)

- To select for feed efficiency
- We calculate EBVs for DMI, instead of residual traits

Expensive trait to measure

Few records in the beginning

Simple repeatability model



E-chapter 40. Dry matter intake



# Current data

Now we have accumulated  
DMI data from:

+10K Holstein cows

+20K lactations

+1 million DMI records



# Current data

Now we have accumulated  
DMI data from:

+10K Holstein cows

+20K lactations

+1 million DMI records

**Opens opportunity for  
improved modelling!**



# Multi-trait dynamic model for genetic RFI

- Multi-trait  $\Rightarrow$  adjusted by MilkE, MBW and dMBW
- Dynamic  $\Rightarrow$  RRM for traits on lactation day
- Genetic  $\Rightarrow$  adjustment on the genetic level

Islam et al., 2020

Khanal et al., 2022

Stephansen et al., 2023

Houlahan et al., 2023

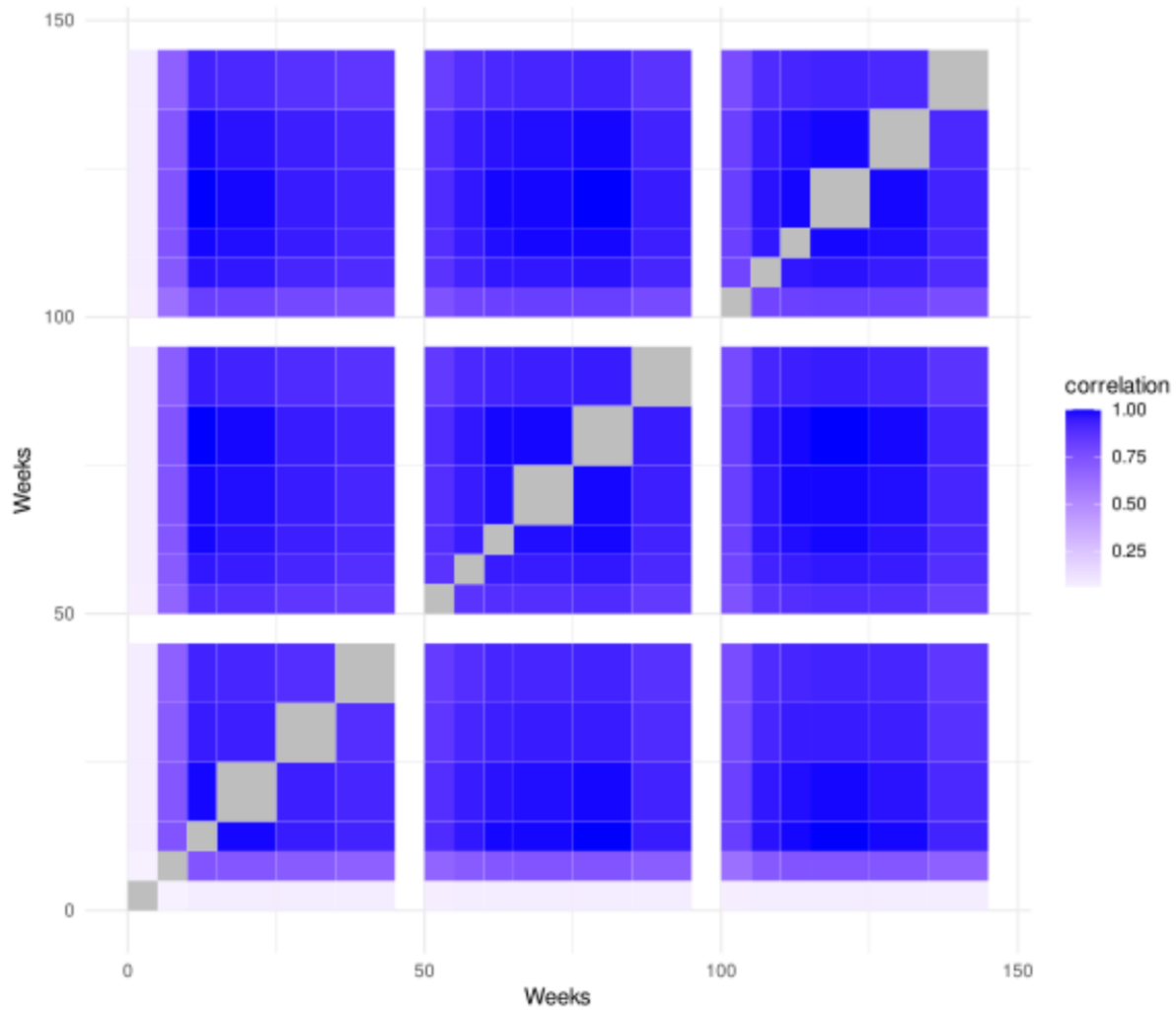
- Requires a dynamic modelling of the DMI genetic component



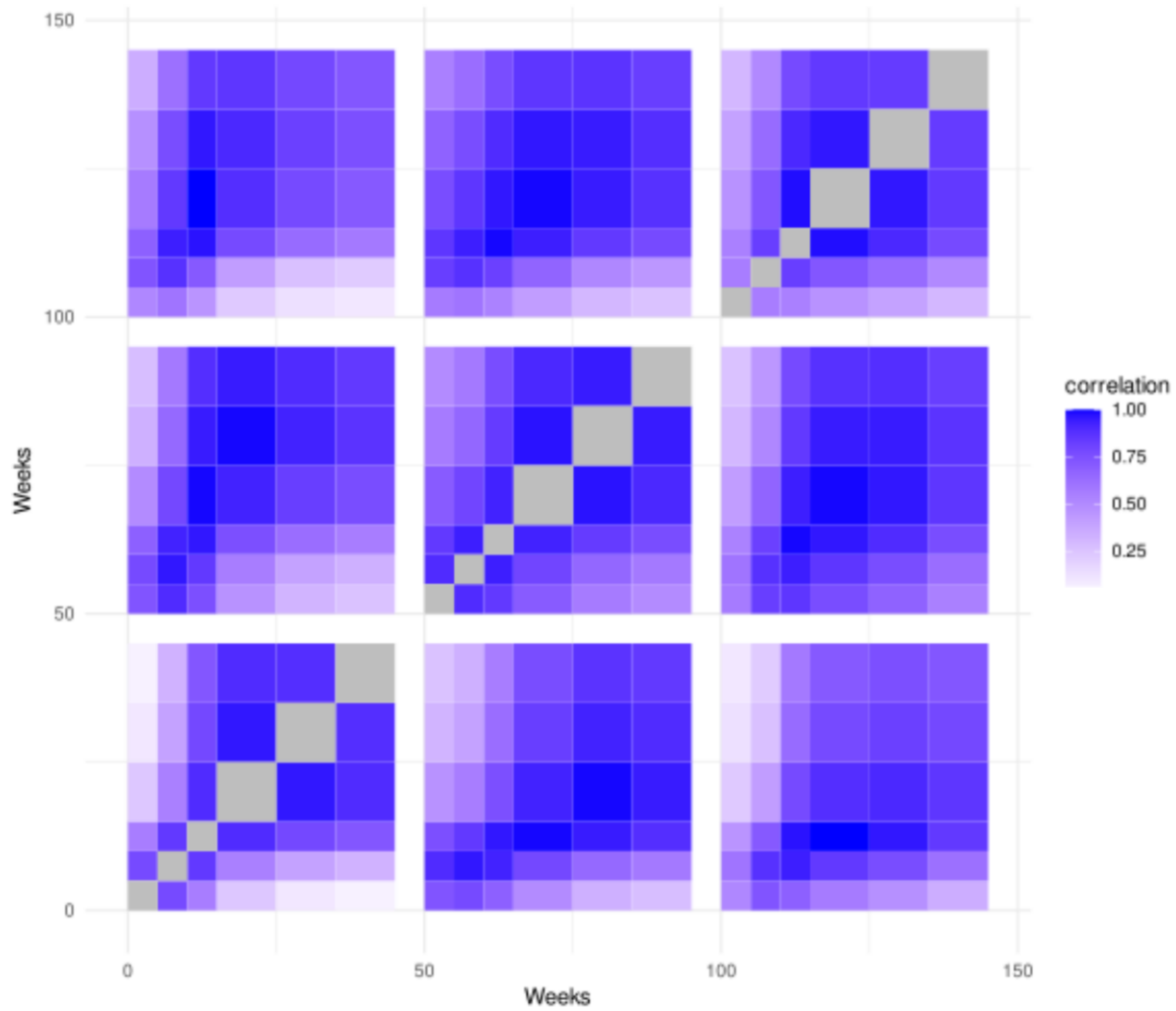
# Improvements in Statistical Software

- Newer versions of ASReml
  - XFA parameterization for variance structures
  - Allows for incremental increase in complexity

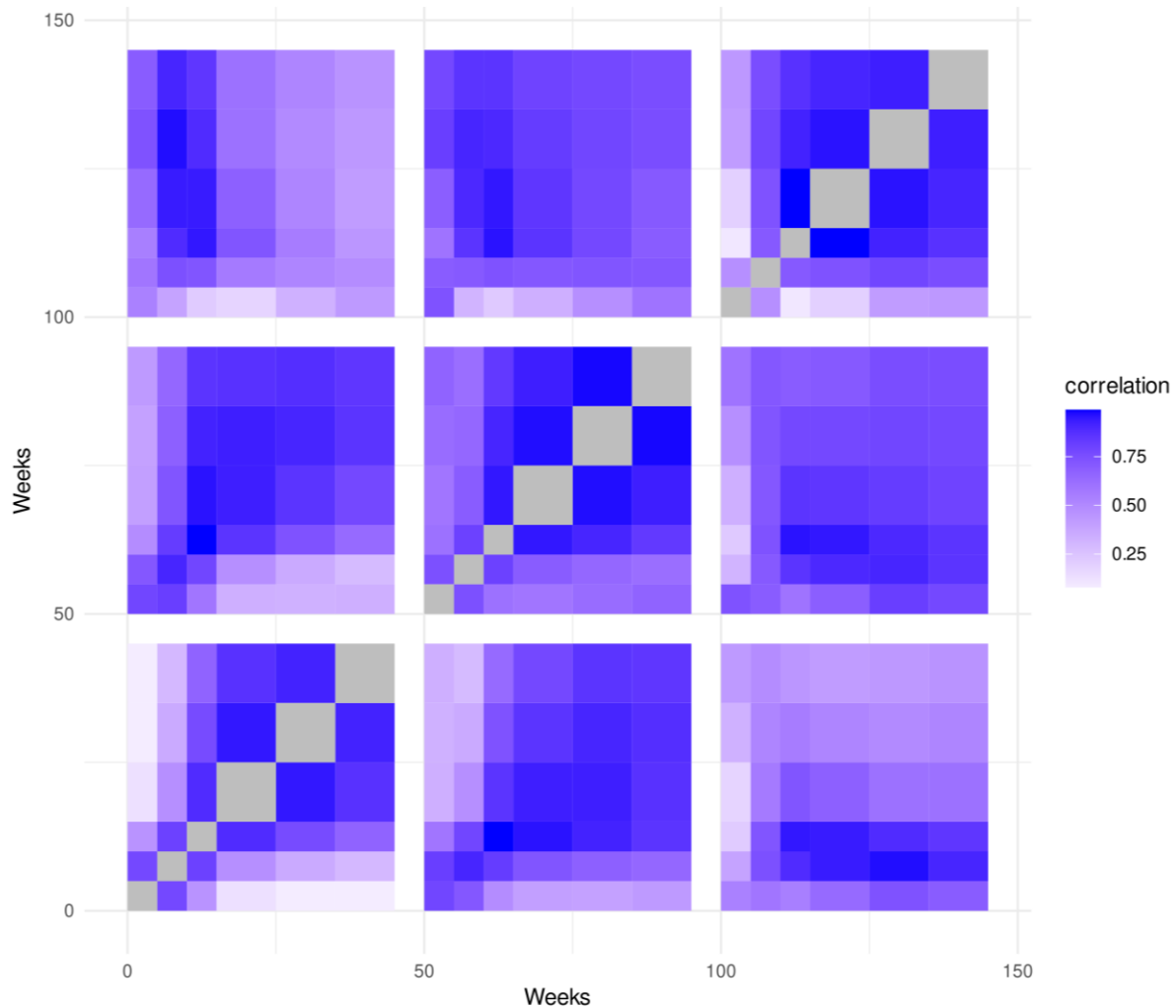
Correlations of DMI ebvs across weeks and parities (1 factor)



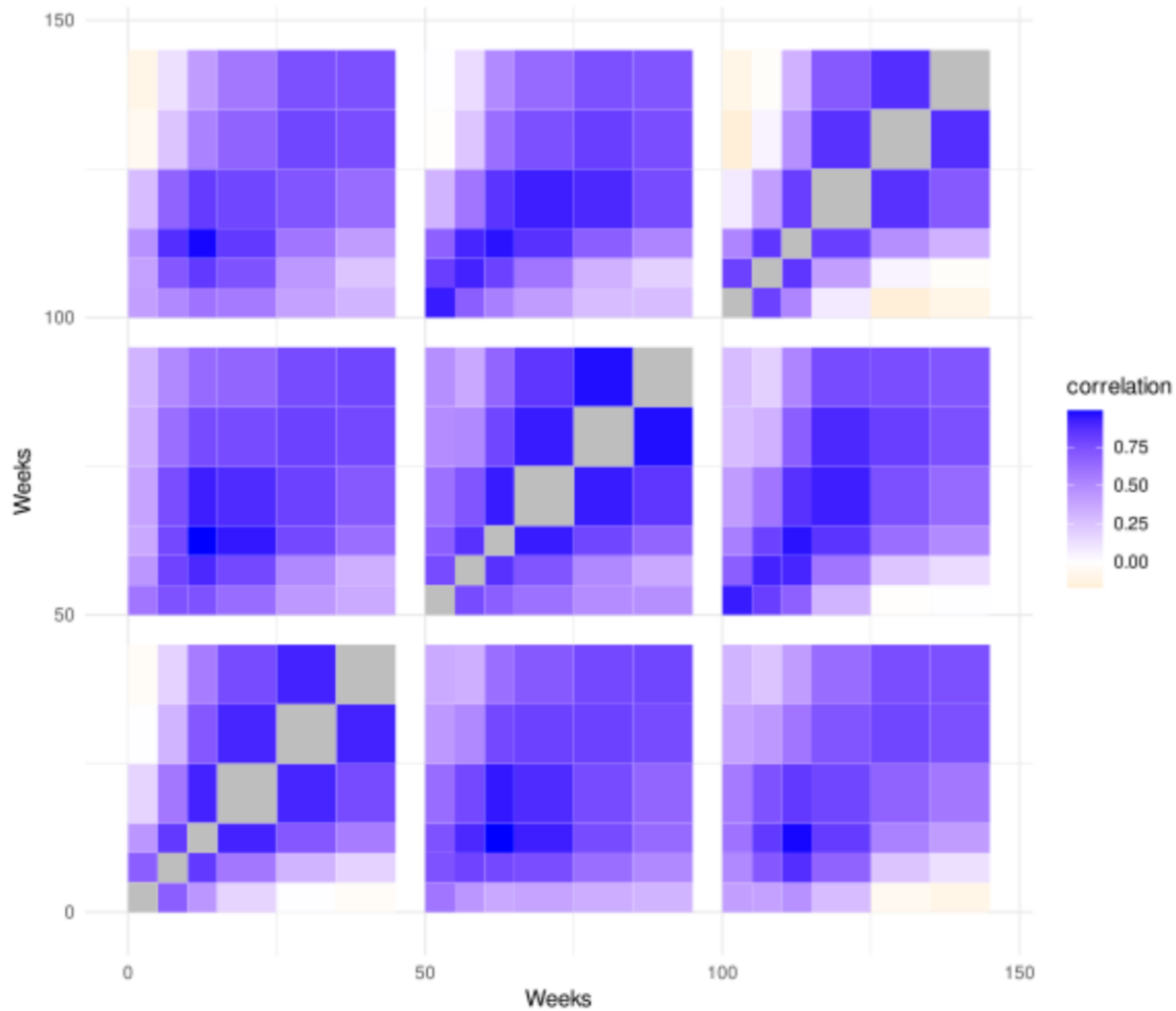
Correlations of DMI ebvs across weeks and parities (2 factors)



Correlations of DMI ebvs across weeks and parities (3 factors)

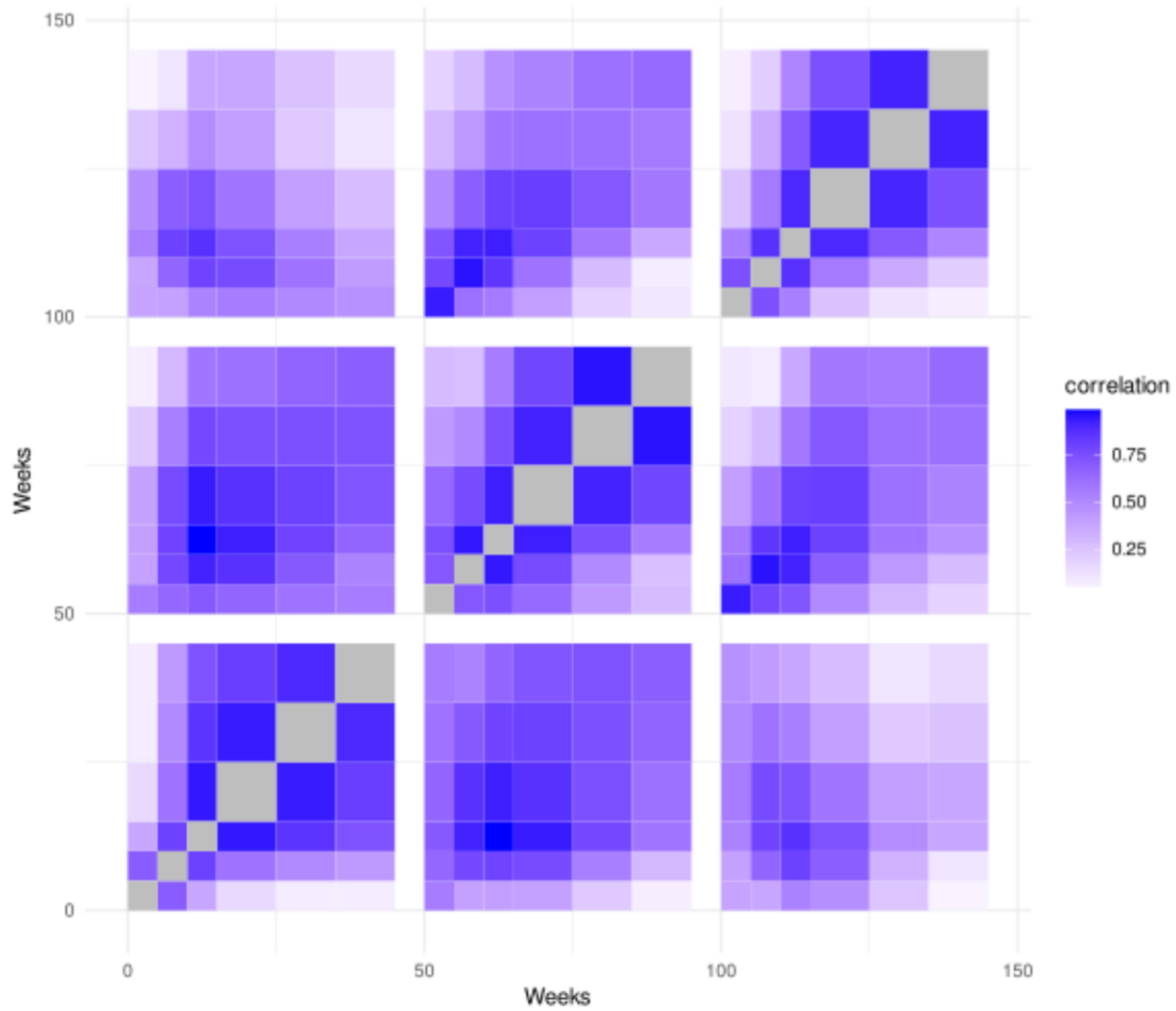


Correlations of DMI ebvs across weeks and parities (4 factors)

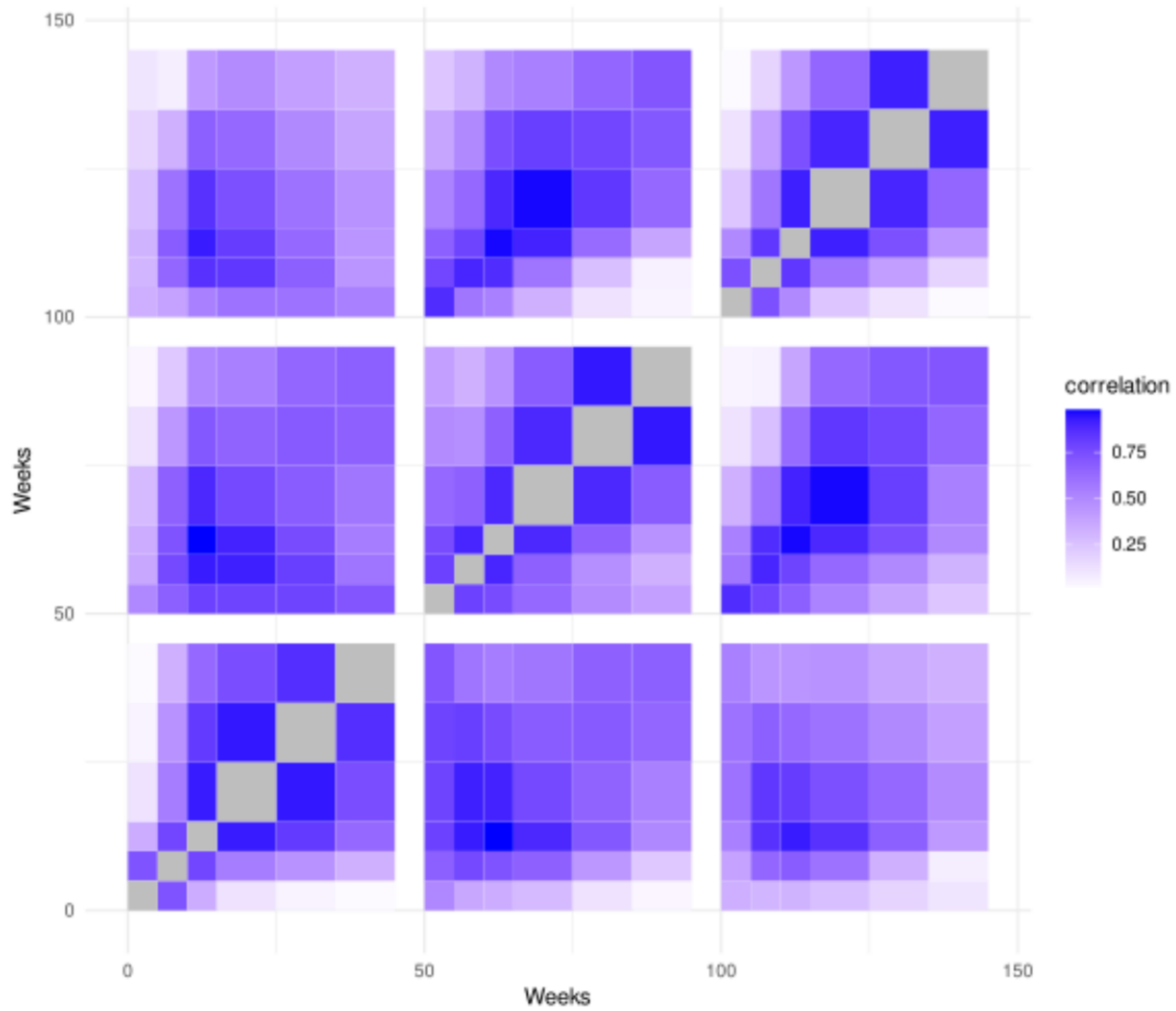




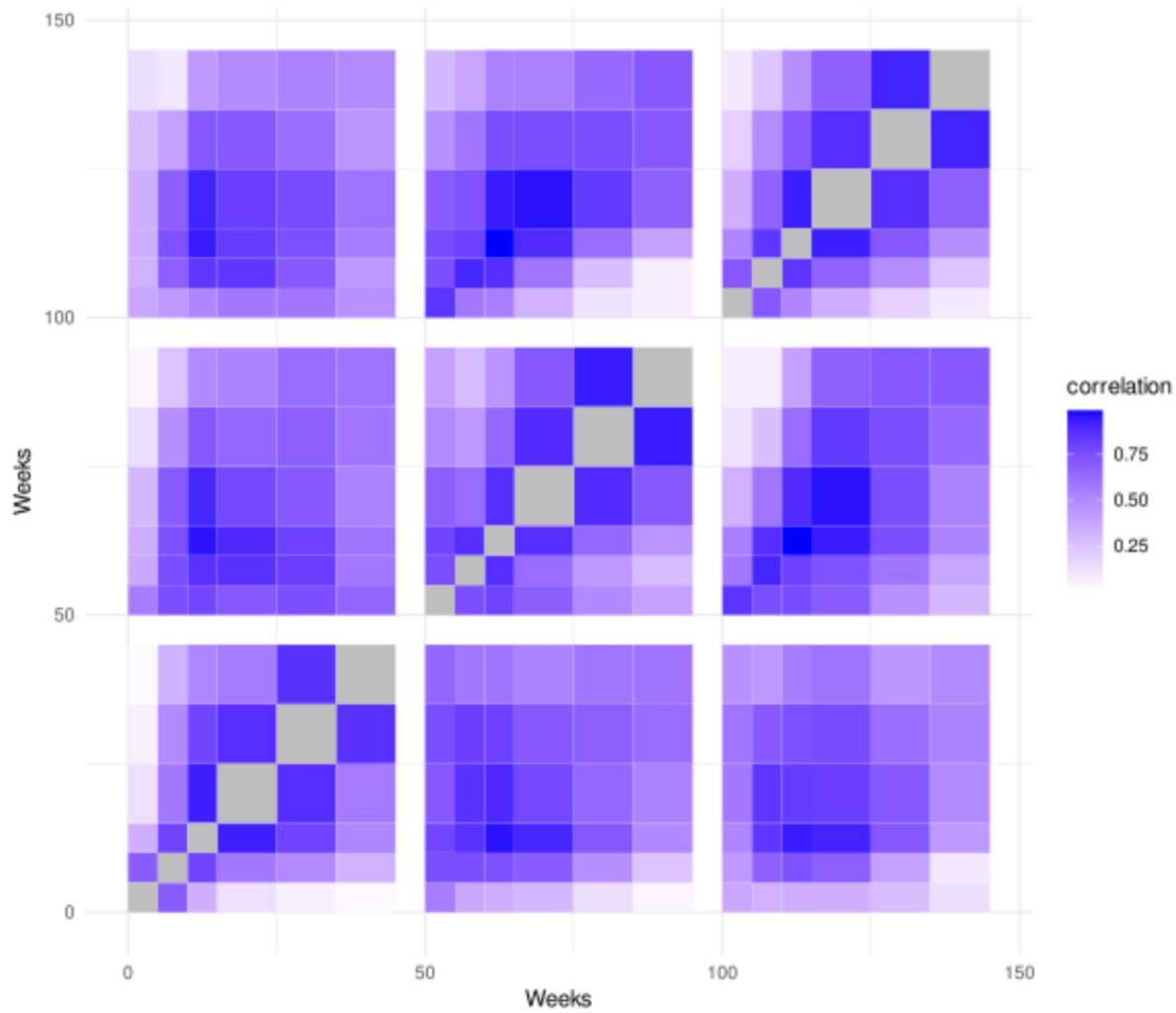
Correlations of DMI ebvs across weeks and parities (5 factors)



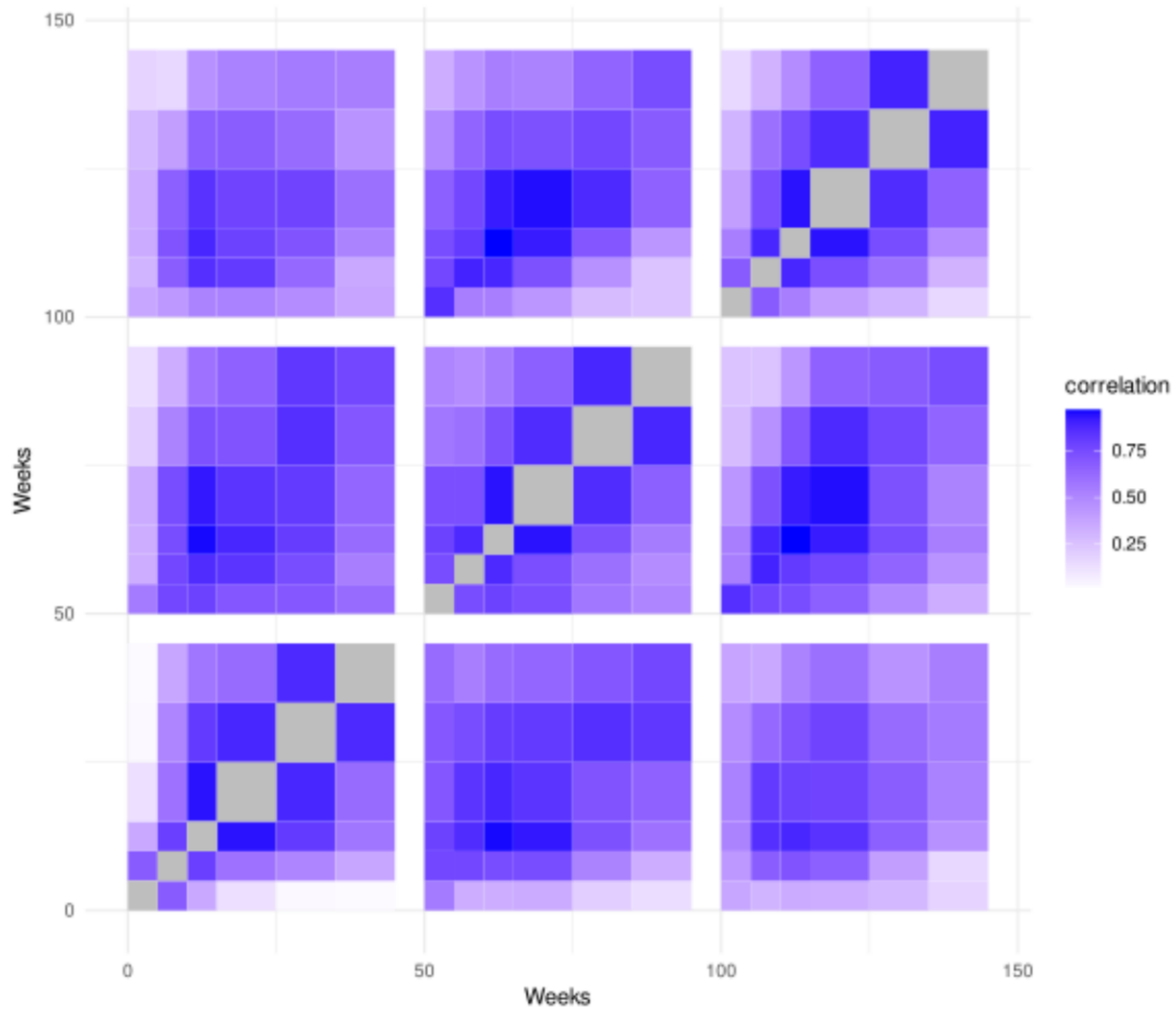
Correlations of DMI ebvs across weeks and parities (6 factors)



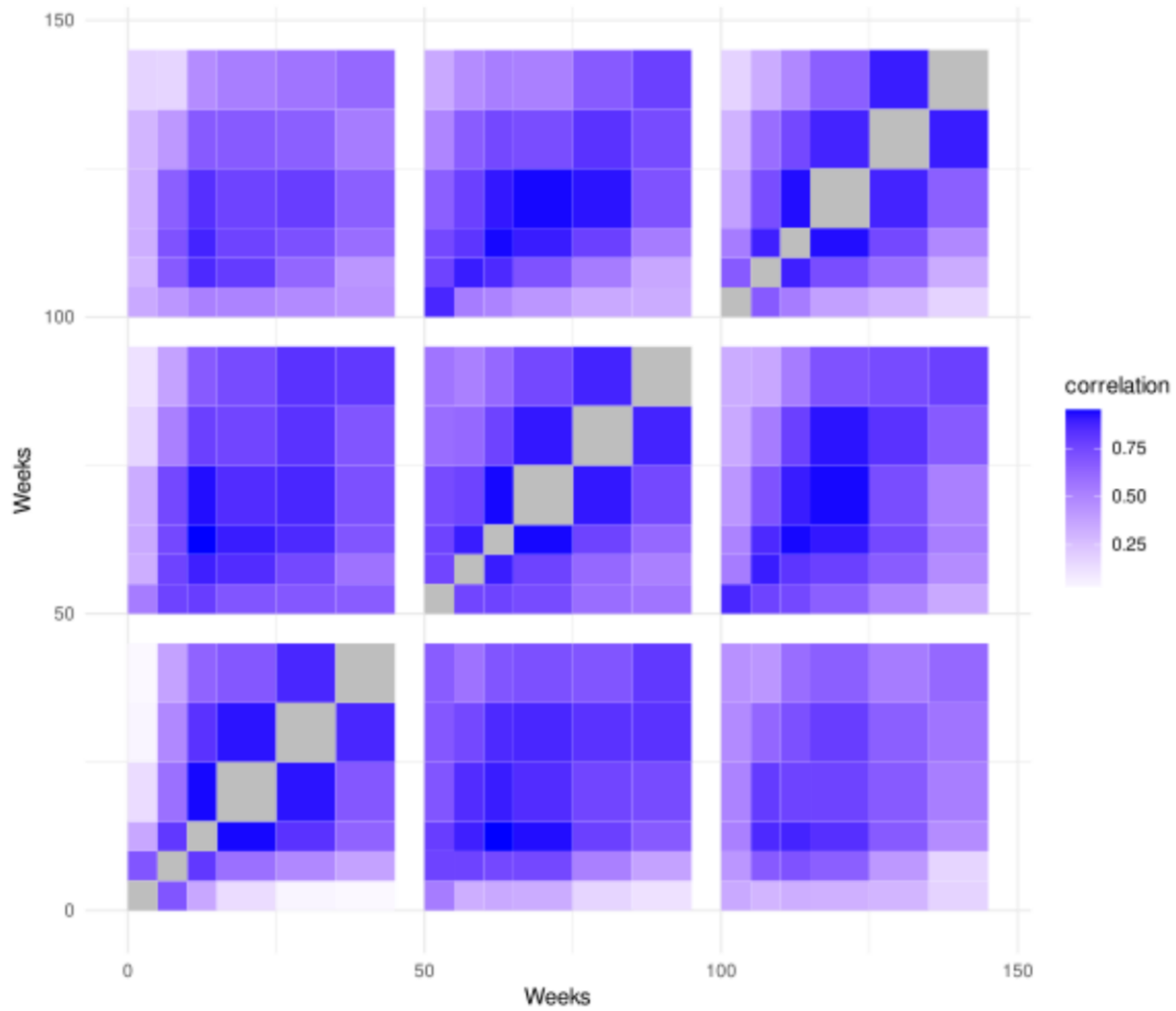
Correlations of DMI ebvs across weeks and parities (7 factors)



Correlations of DMI ebvs across weeks and parities (8 factors)

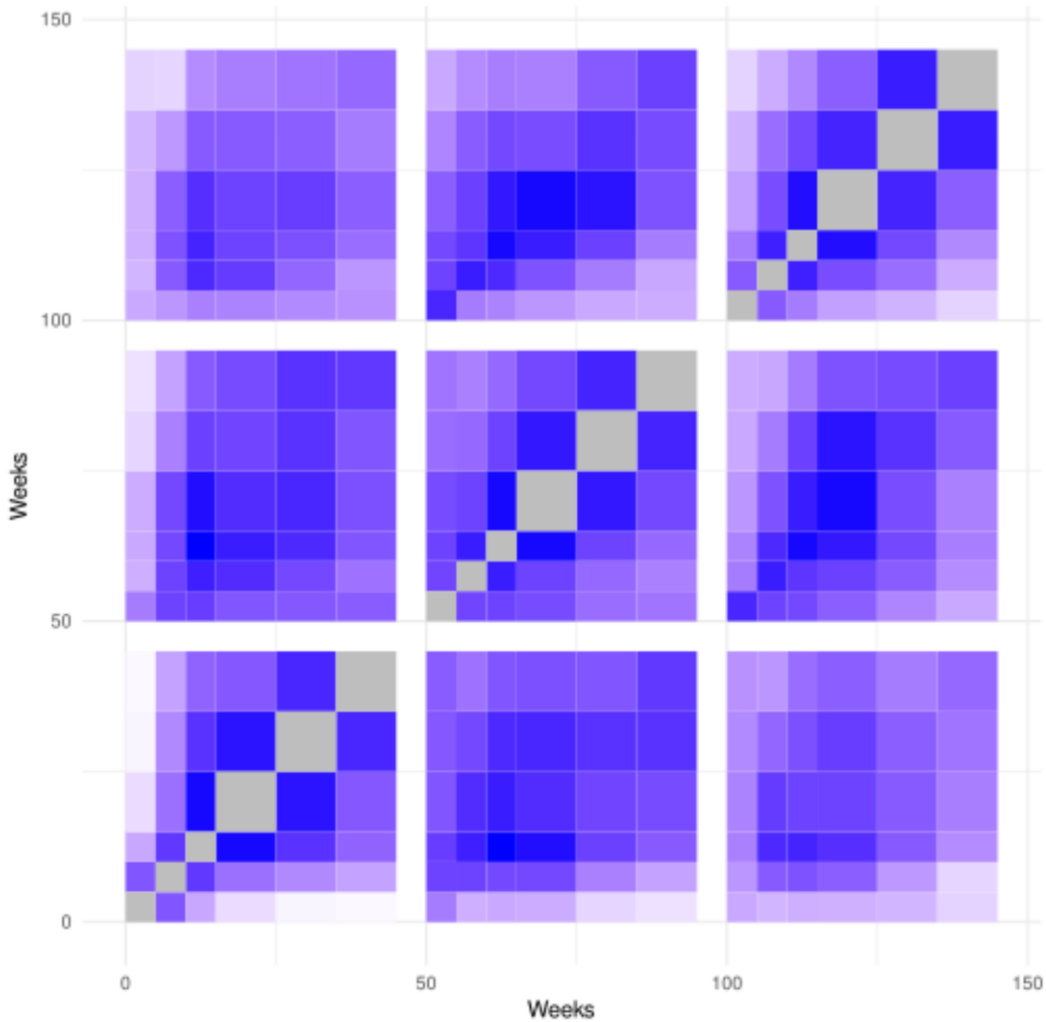


Correlations of DMI ebvs across weeks and parities (9 factors)

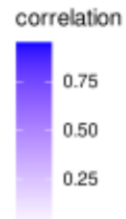




Correlations of DMI ebvs across weeks and parities (9 factors)



*i405 parameters  
estimated in the  
covariance  
matrix!*



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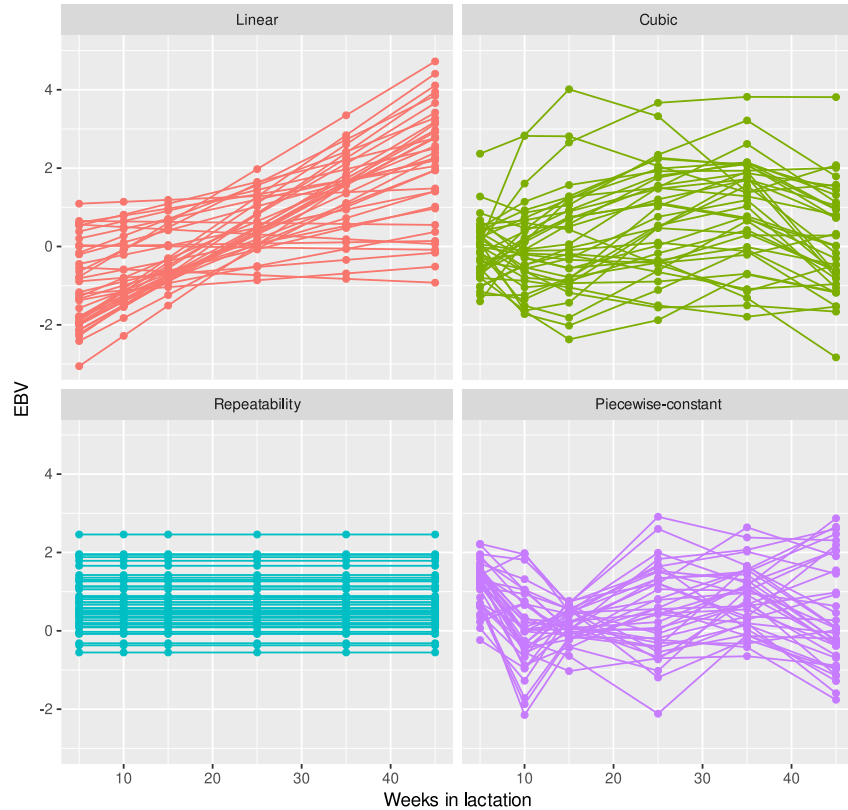
- Newer versions of **ASReml**
  - XFA parameterization for variance structures
  - Allows for incremental increase in complexity
  
- Newer versions of **MixBLUP**
  - efficient ssSNPBLUP running on GPUs

# Random Regression Models

# Random Regression Model

Random regressions  
on days in milk (nested in parity)

- Linear
- Cubic
- Repeatability
- Piecewise-constant





# Cross-Validation Assessment

# Validation approaches

- Parametric
  - Likelihood, AIC, BIC
  
- Non-parametric
  - CV on DRPs

# Validation approaches

- Parametric
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- Semi-parametric
  - LR-method
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## Semi-parametric

Compares EBVs from partial data,  
with EBVs from full data.

Model	rho	mse
Linear	0.25	1.09
Cubic	0.20	1.03
Repeatability	0.28	0.65
Piecewise-constant	0.41	0.48

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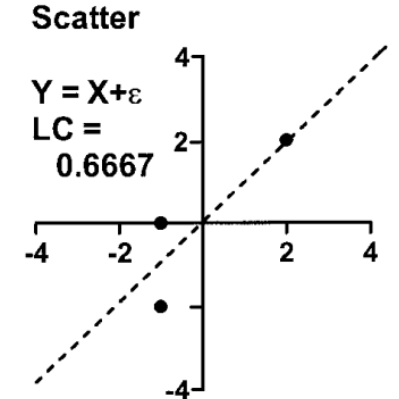
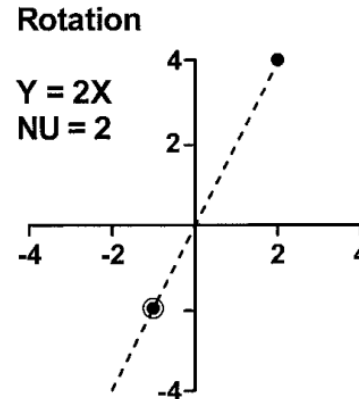
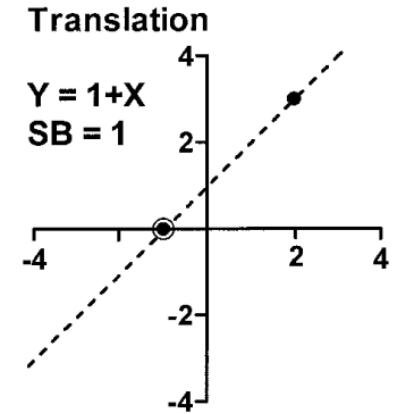
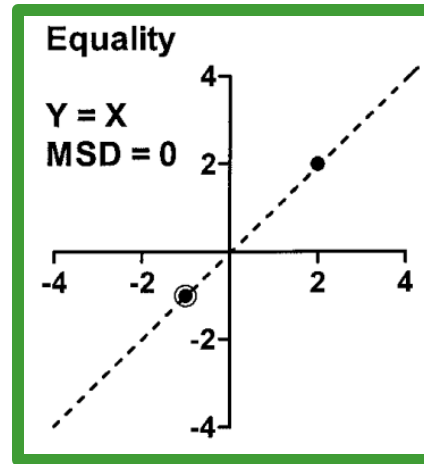
 Used PWC model  
fitted with full data  
as the prediction target

# Validation metrics

## Possible discrepancies

- Level bias -> SB
- Inflation/deflation -> NU
- Accuracy -> LC

$$\text{MSE} = \text{SB} + \text{NU} + \text{LC}$$



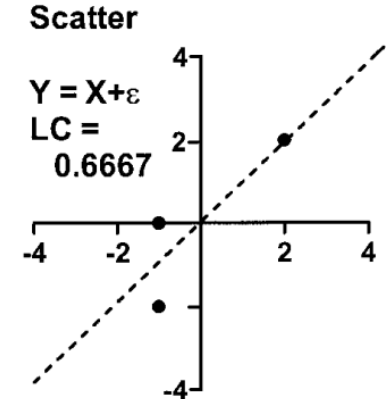
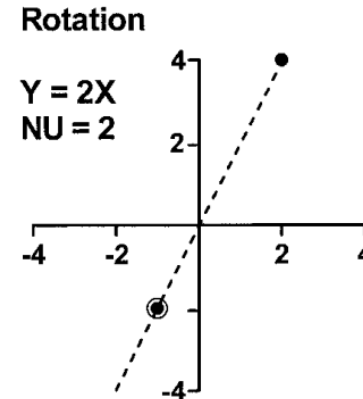
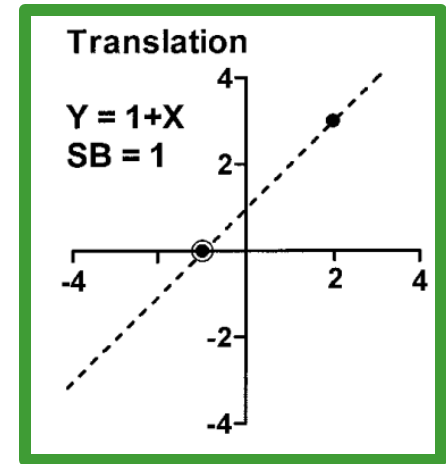
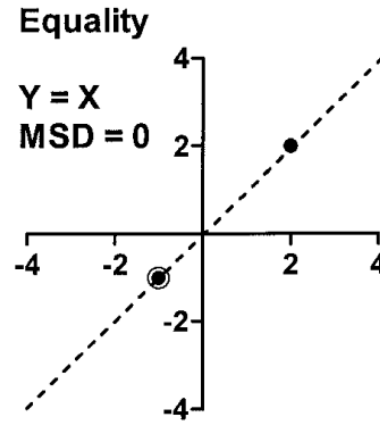
Gauch et al., 2003

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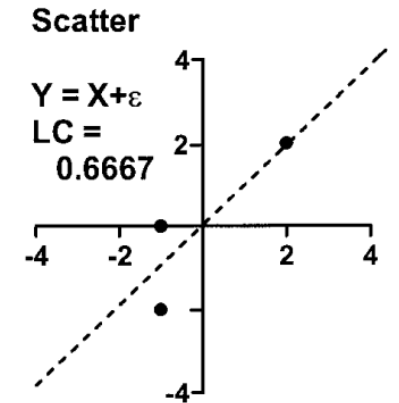
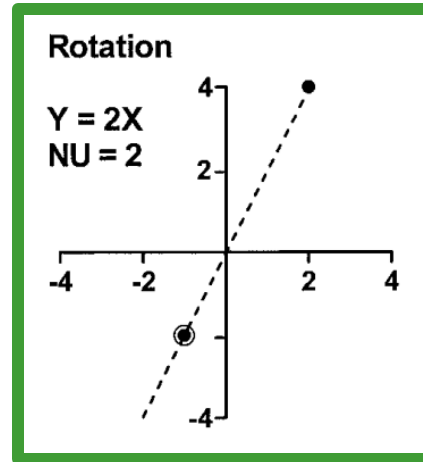
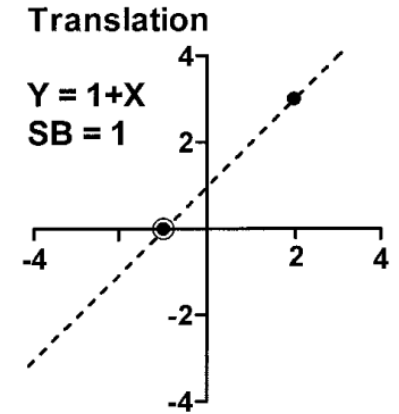
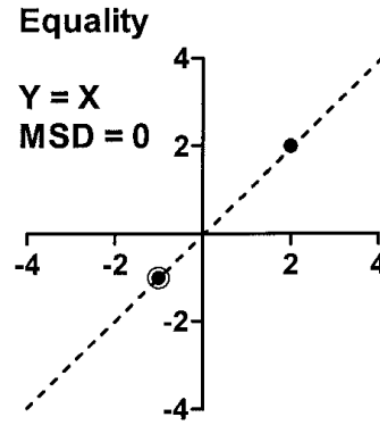
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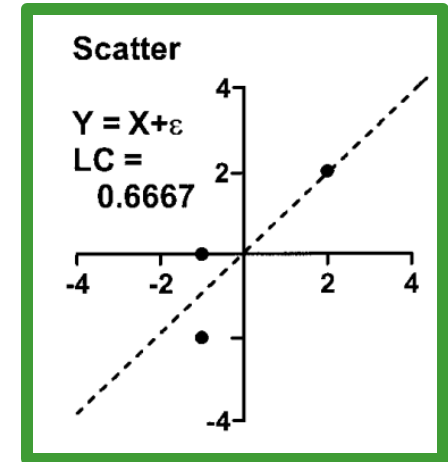
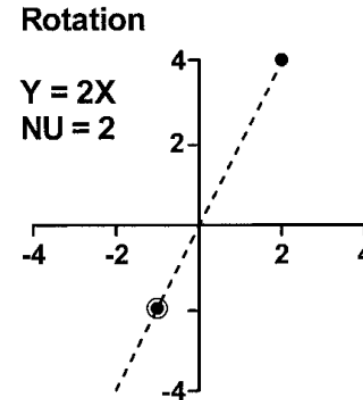
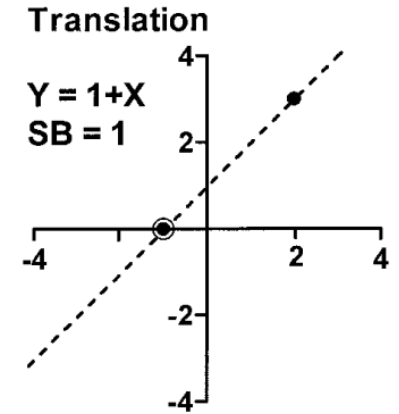
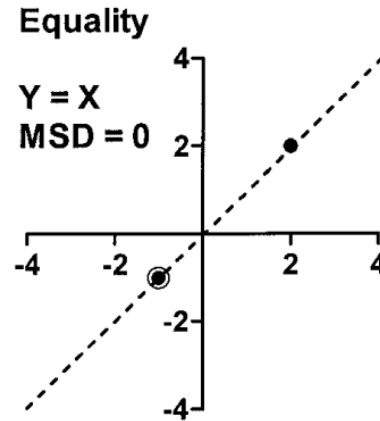


# Validation metrics

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Gauch et al., 2003

# Validation metrics

Possible discrepancies

- Level bias -> SB
- Inflation/deflation -> NU
- Accuracy -> LC

$$\mathbf{MSE} = \mathbf{SB} + \mathbf{NU} + \mathbf{LC}$$

$$\mathbf{LB} = (\bar{X} - \bar{Y})^2$$

$$\mathbf{NU} = (1 - b)^2 V_X$$

$$\mathbf{LC} = (1 - \rho^2) V_Y$$

# Forward validation

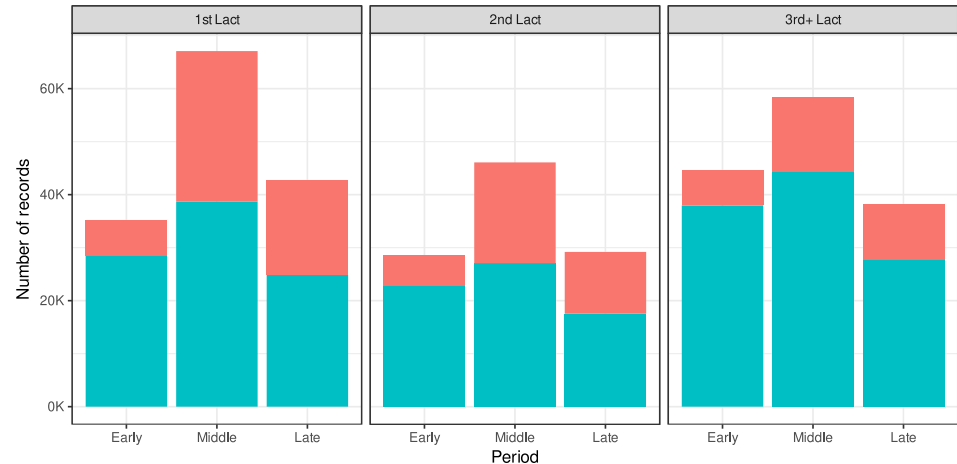
Cutoff date: 2020

Disclaimer: pedigree blups shown here

- Focal groups
  - validation cows, (0 records in partial , +3 in full) #2958
  - young sires, (0 phenotyped daughters in partial, +10 in full) #41
  - proven sires, (+10 phenotyped daughters in partial, +1 in full) #38

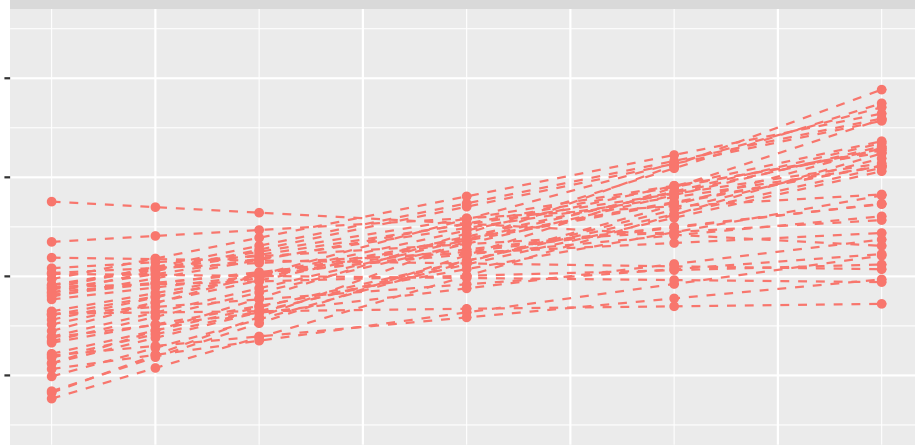
- Lactation periods

- Early (weeks 5 & 10)
- Middle (weeks 15 & 25)
- Late (weeks 35 & 45)

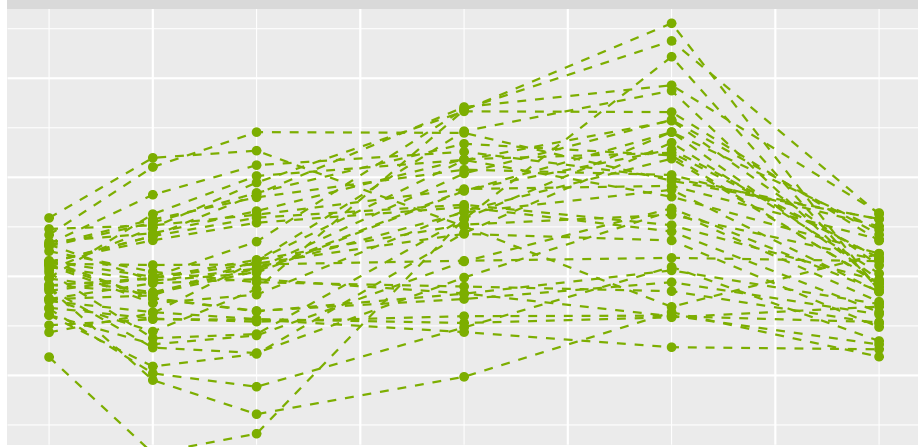


# EBVs proven sires (1st lactation)

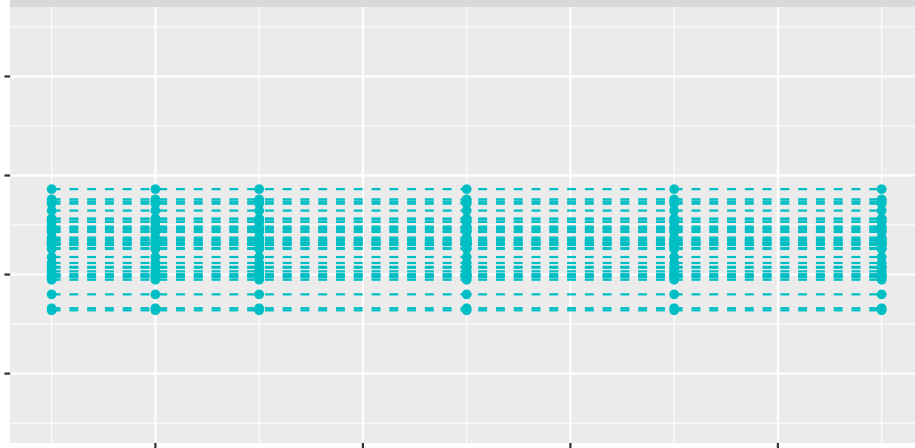
## Linear



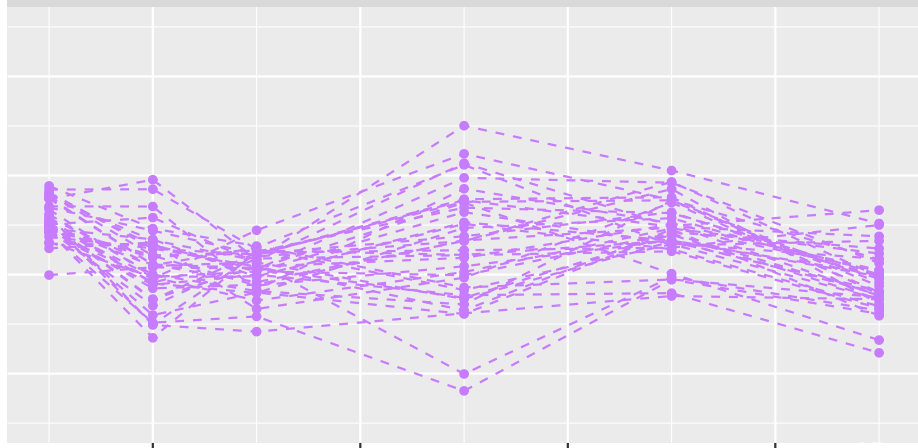
## Cubic



## Repeatability



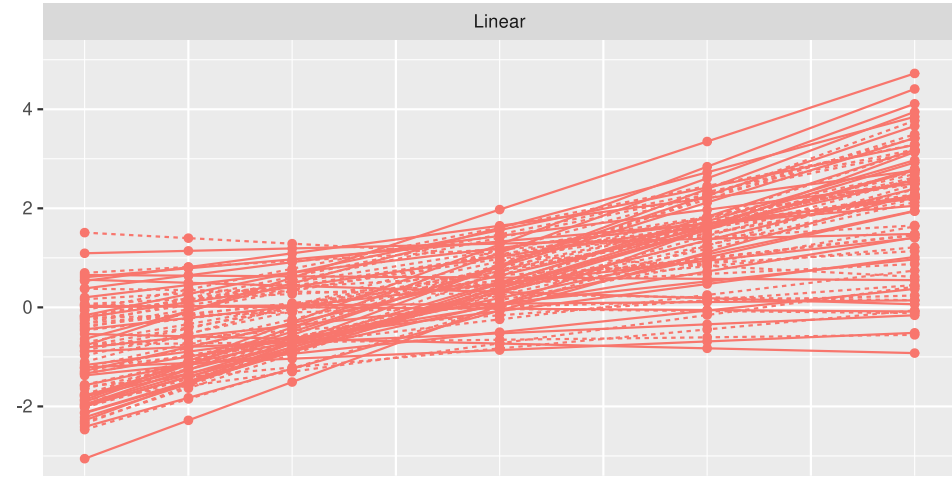
## Piecewise-constant



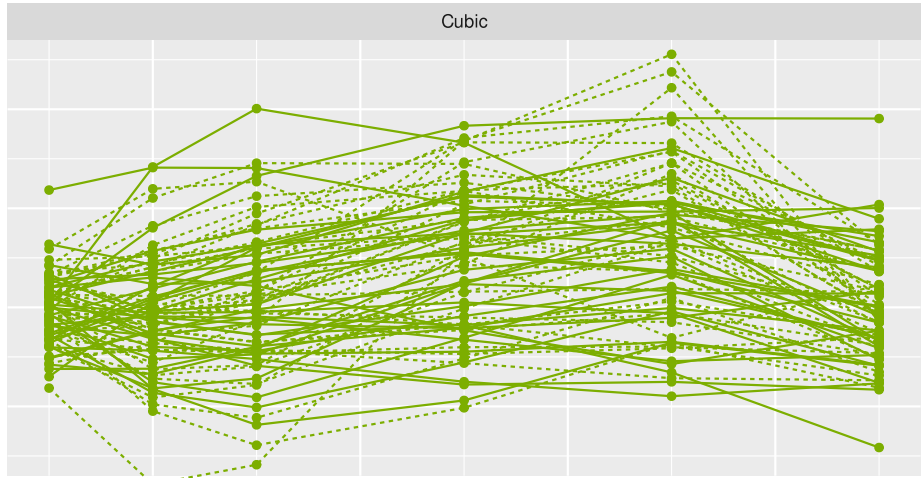
Weeks in lactation

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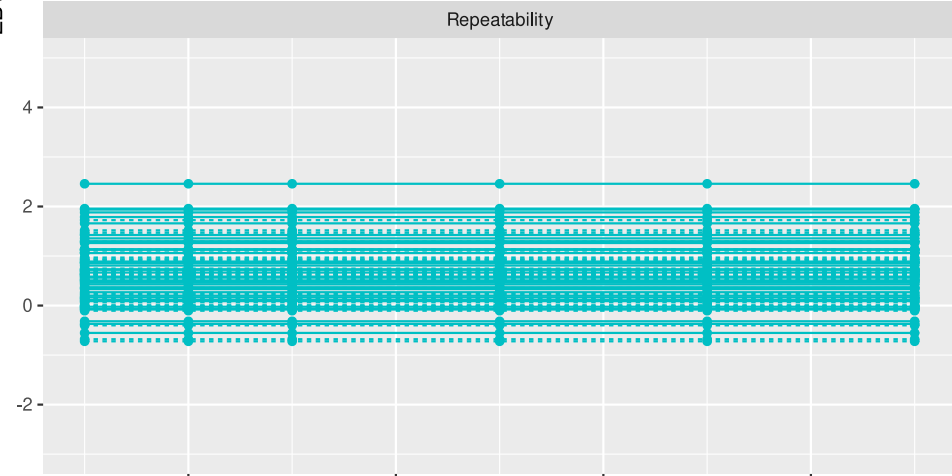
## Linear



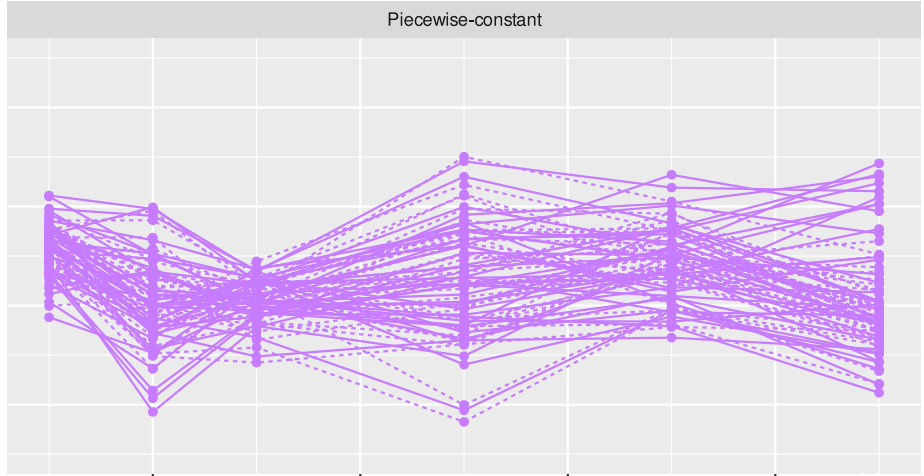
## Cubic



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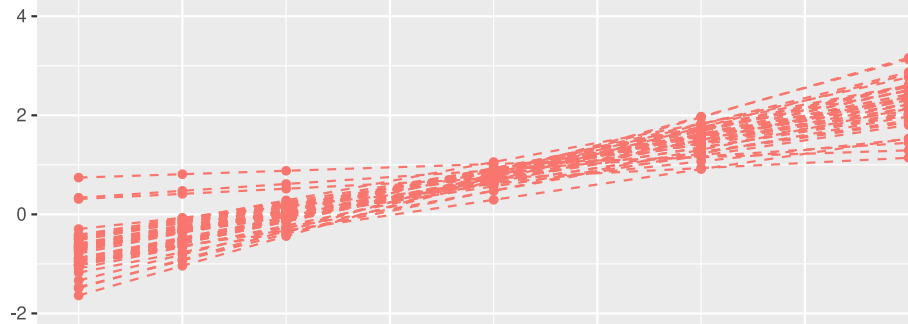
## Piecewise-constant



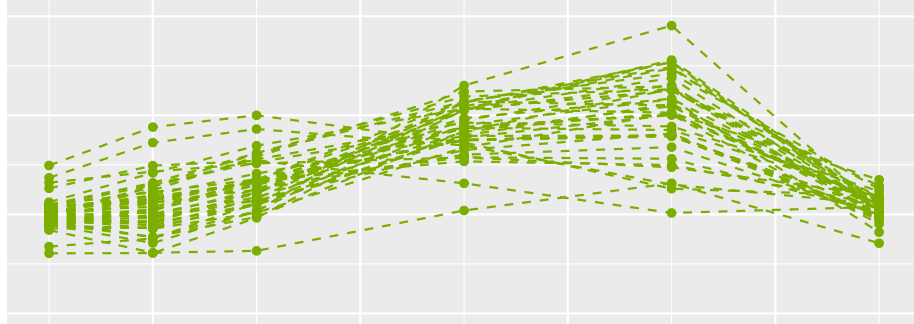
Weeks in lactation

# EBVs young sires (1st lactation)

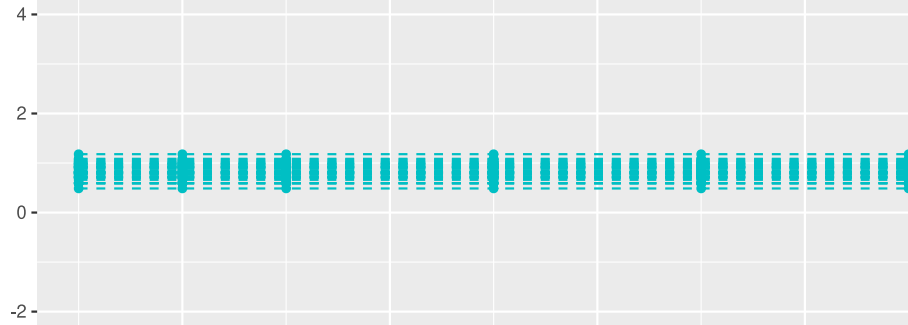
## Linear



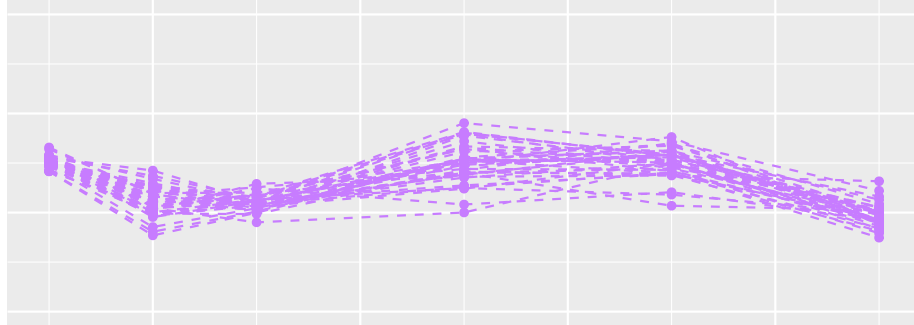
## Cubic



## Repeatability



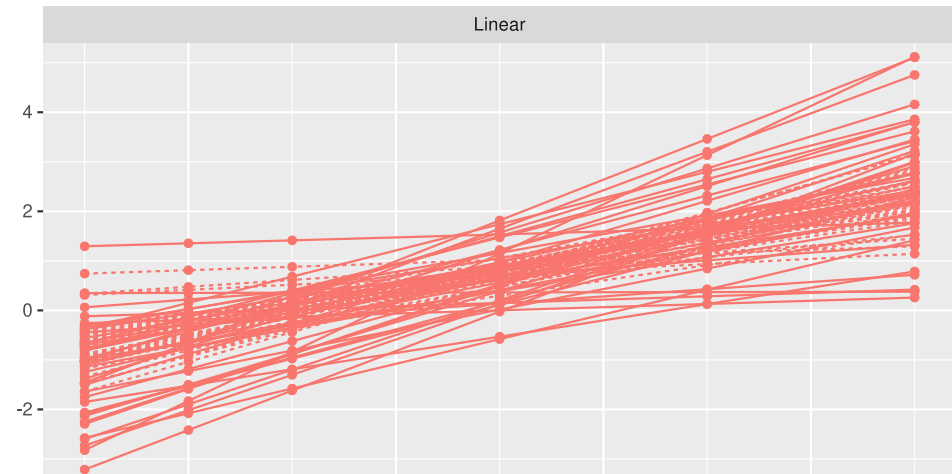
## Piecewise-constant



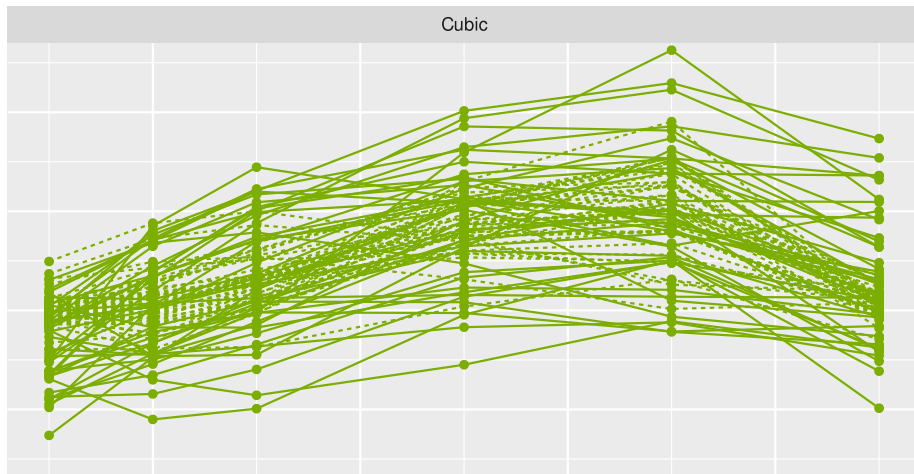
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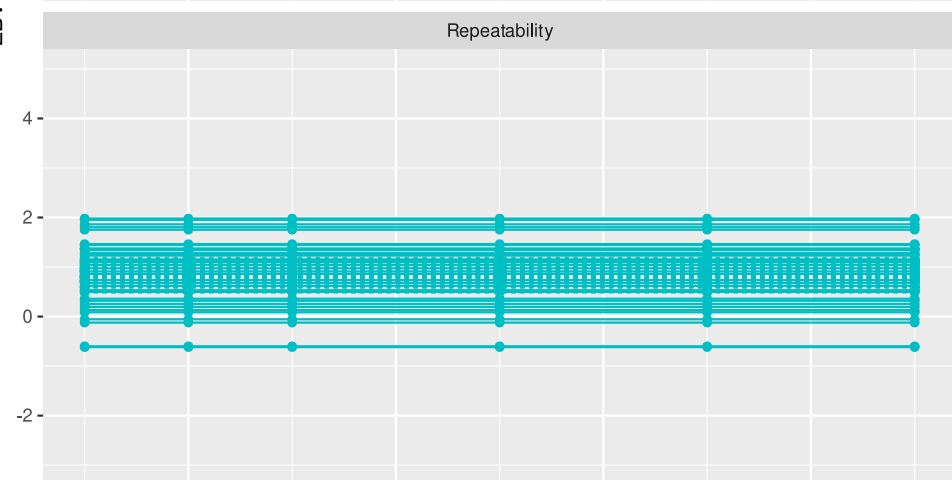
## Linear



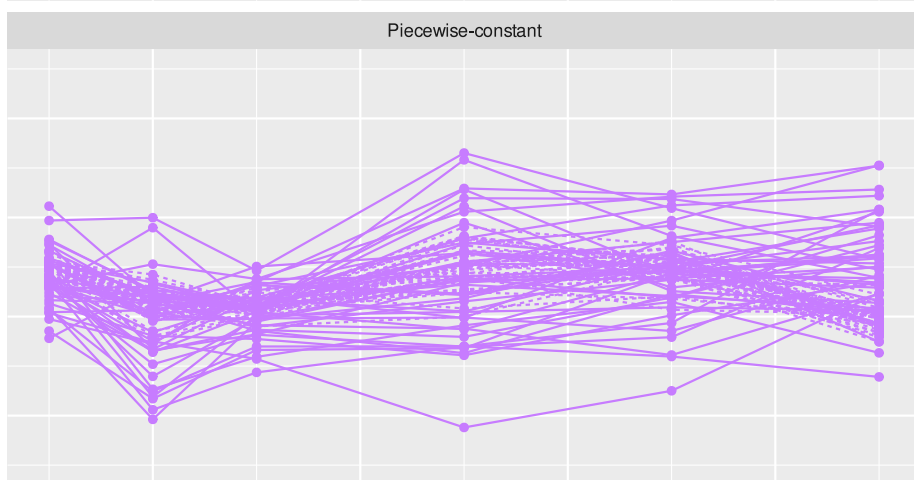
## Cubic



## Repeatability



## Piecewise-constant

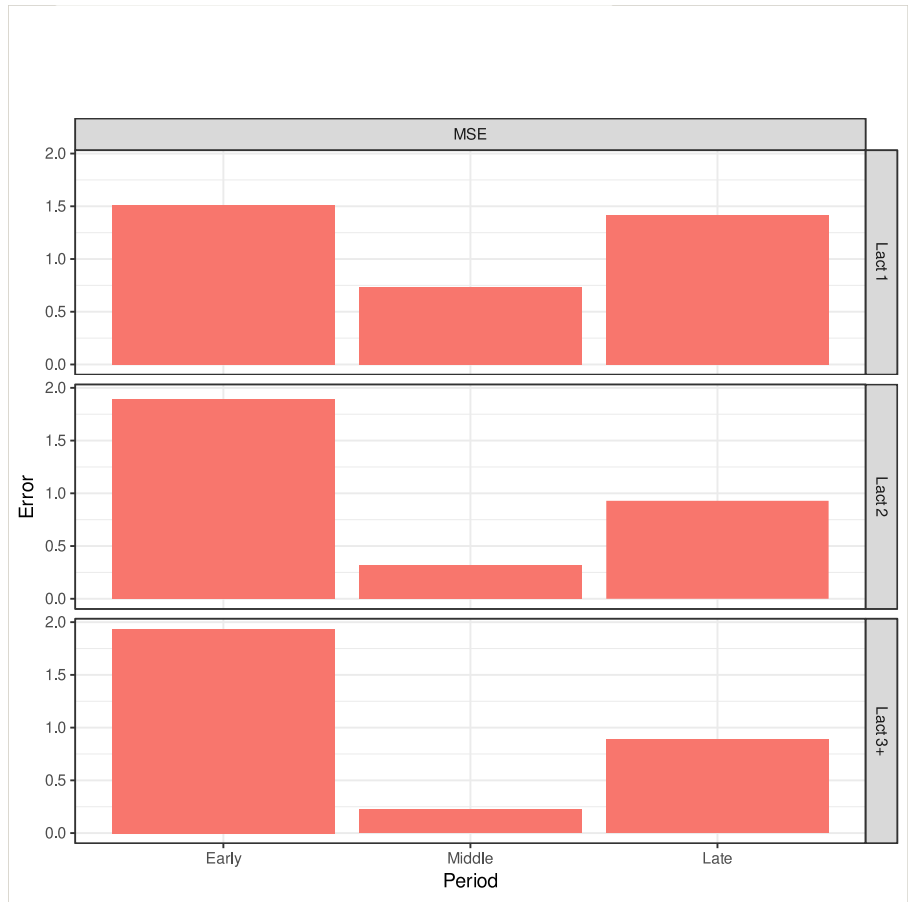


Weeks in lactation

# Forward validation for Linear RRM

Simple model predicts well in middle of lactation

And poorly in early and late periods

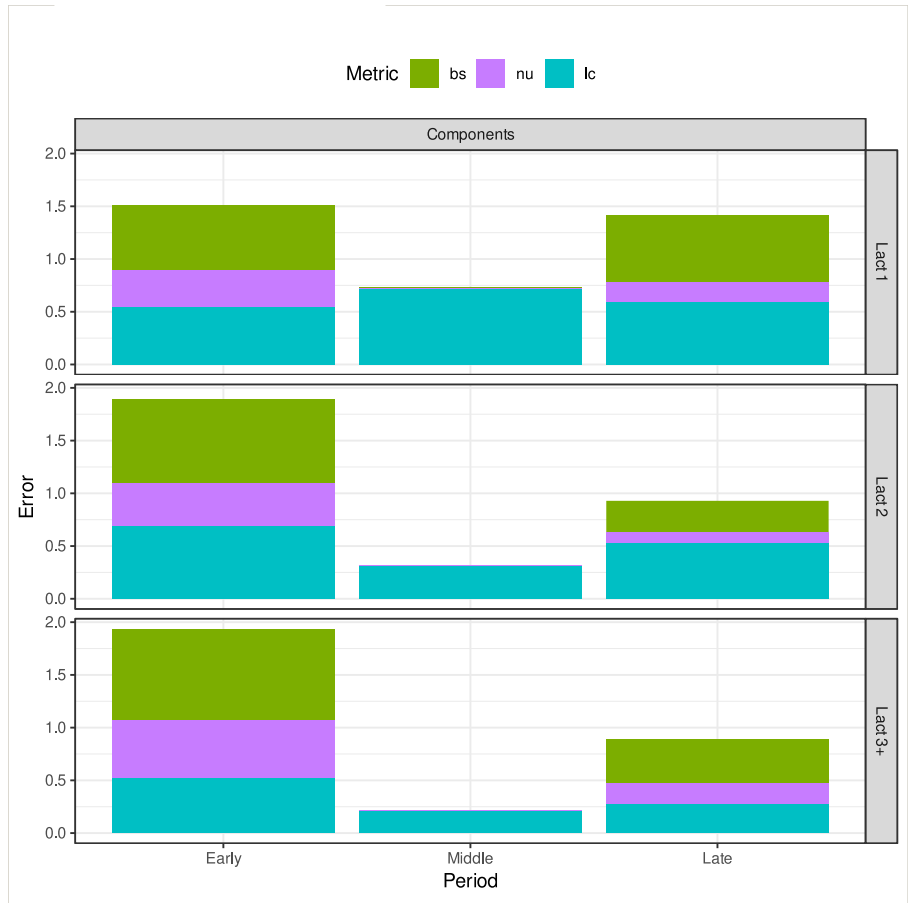




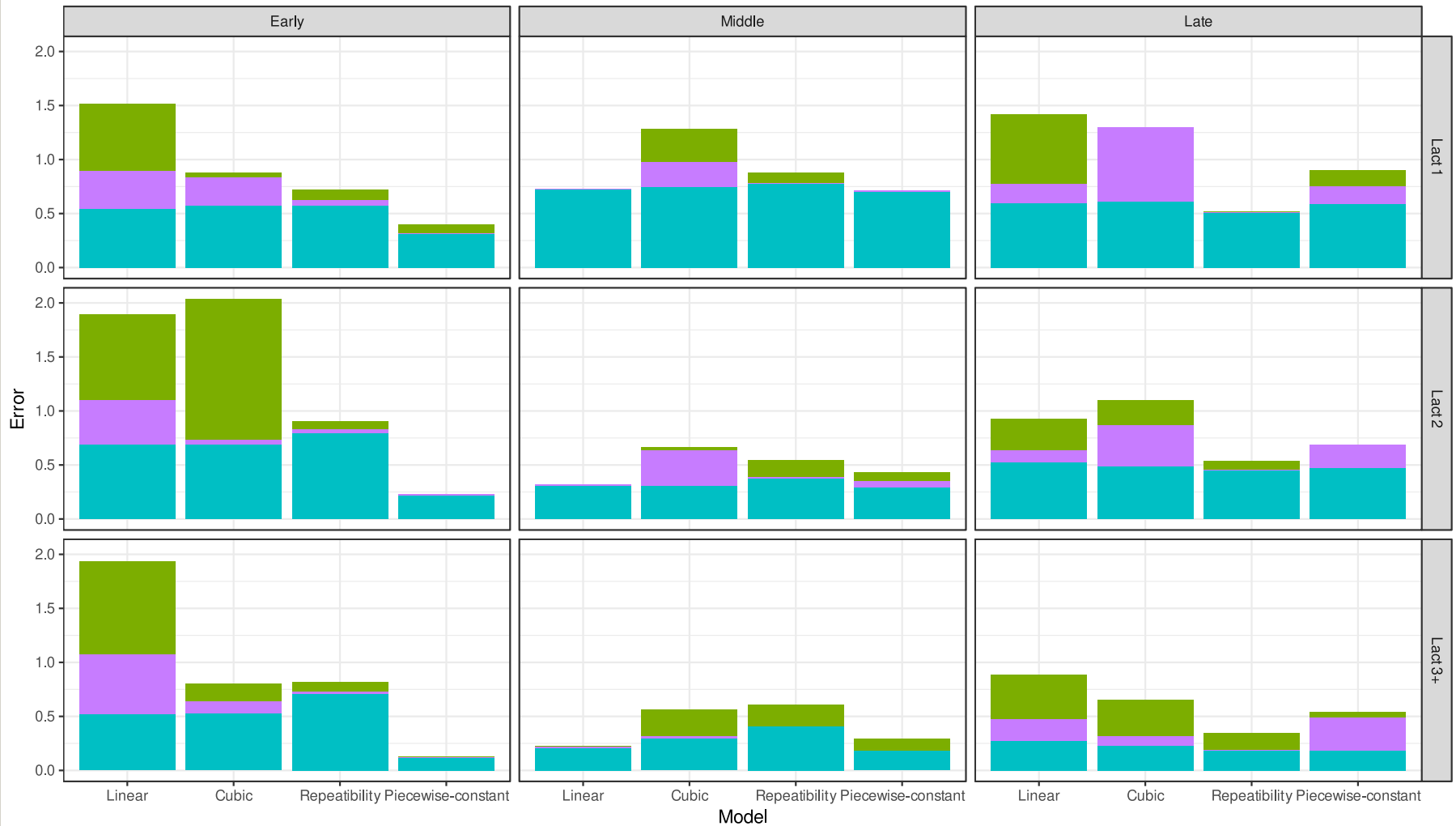
# MSE partitioned into components

Level bias due to systematic under- and over-predictions in the extremes of the range

Accuracy is also lower in the middle period, only for 2+ lact.



# Forward validation (target: PWC)



# Discussion

- Cross-validation is crucial for assessing predictive performance
- Predictive accuracy will vary throughout the lactation
- Separating MSE into components can assist interpretation

# Discussion

- Other basis for the RRM can be explored (e.g. splines)
- Could PWC be entertained for the evaluation?
  - Against which model could it be validated?
- Different criteria for focal animals may be considered
- Uncertainty in validation metrics should be included

# Thanks for your attention!

Questions and comments?  
Remember, work in progress,  
Suggestions are welcome.

